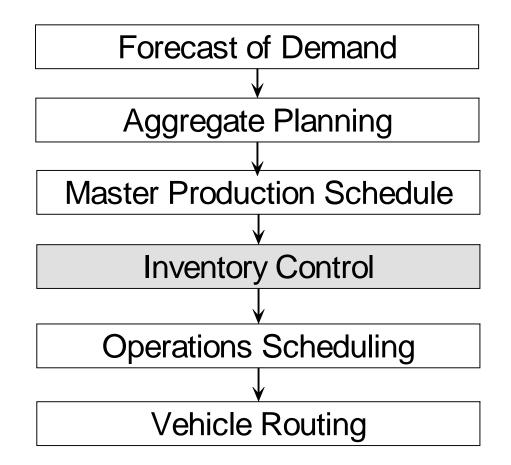
### LESSON 21: MATERIAL REQUIREMENTS PLANNING

#### Outline

- Hierarchy of Production Decisions
- MRP and its importance
- Input and Output of an MRP system
- MRP Calculation
- Lot Sizing
- Lot Sizing with Capacity Constraint

- The next slide presents a schematic view of the aggregate production planning function and its place in the hierarchy of the production planning decisions.
- Forecasting: First, a firm must forecast demand for aggregate sales over the planning horizon.
- Aggregate planning: The forecasts provide inputs for determining aggregate production and workforce levels over the planning horizon.
- Master production schedule (MPS): Recall, that the aggregate production plan does not consider any "real" product but a "fictitious" aggregate product. The MPS translates the aggregate plan output in terms of specific production goals by product and time period. For example,



suppose that a firm produces three types of chairs: ladderback chair, kitchen chair and desk chair. The aggregate production considers a fictitious aggregate unit of chair and find that the firm should produce 550 units of chairs in April. The MPS then translates this output in terms of three product types and four work-weeks in April. The MPS suggests that the firm produce 200 units of desk chairs in Week 1, 150 units of ladder-back chair in Week 2, and 200 units of kitchen chairs in Week 3.

 Material Requirements Planning (MRP): A product is manufactured from some components or subassemblies.
 For example a chair may require two back legs, two front legs, 4 leg supports, etc. While forecasting, aggregate plan

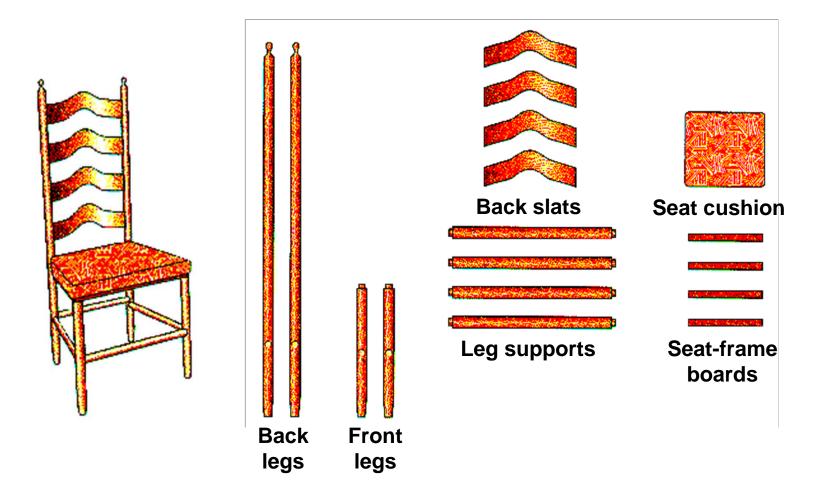
### Hierarchy of Production Decisions Master Production Schedule

		Αρ	oril		Мау						
	1	2	3	4	5	6	7	8			
Ladder-back chair		150				150					
Kitchen chair			200		120			120			
Desk chair	200				200		200				
Aggregate production plan for chair family		55	50		790						

and MPS consider the volume of finished products, MRP plans for the components, and subassemblies. A firm may obtain the components by in-house production or purchasing. MRP prepares a plan of in-house production or purchasing requirements of components and subassemblies.

- Scheduling: Scheduling allocates resource over times in order to produce the products. The resources include workers, machines and tools.
- Vehicle Routing: After the products are produced, the firm may deliver the products to some other manufacturers, or warehouses. The vehicle routing allocates vehicles and prepares a route for each vehicle.

### Hierarchy of Production Decisions Materials Requirement Planning

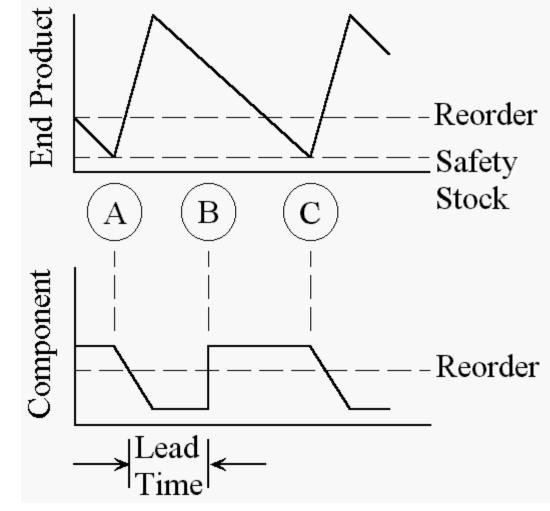


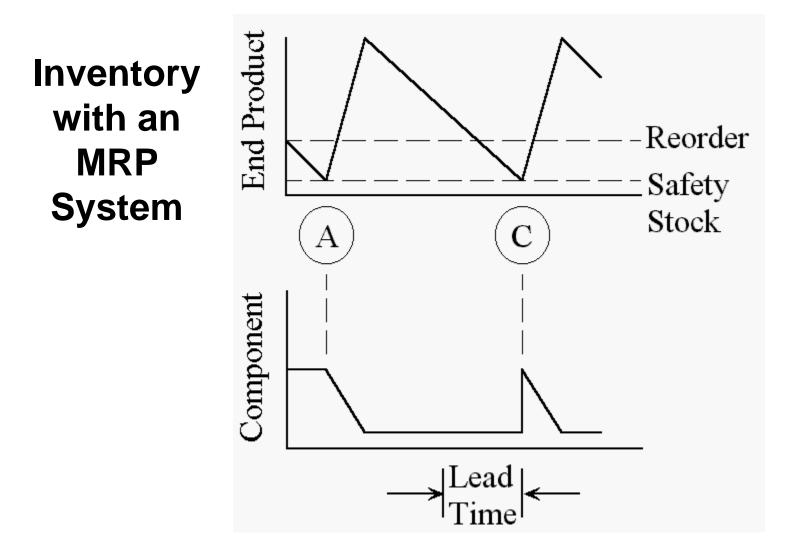
### **Material Requirements Planning**

- The demands for the finished goods are obtained from forecasting. These demands are called independent demand.
- The demands for the components or subassemblies depend on those for the finished goods. These demands are called dependent demand.
- Material Requirements Planning (MRP) is used for dependent demand and for both assembly and manufacturing
- If the finished product is composed of many components, MRP can be used to optimize the inventory costs.

- Next two slides explain the importance of an MRP system. The first one shows inventory levels when an MRP system is not used. The next one shows the same when an MRP system is used.
- The chart at the top shows inventory levels of the finished goods and the chart on the bottom shows the same of the components.
- If the production is stopped (like it is at the beginning of the chart), the finished goods inventory level decreases because of sales. However, the component inventory level remains unchanged. When the production resumes, the finished goods inventory level increases, but the component inventory level decreases.

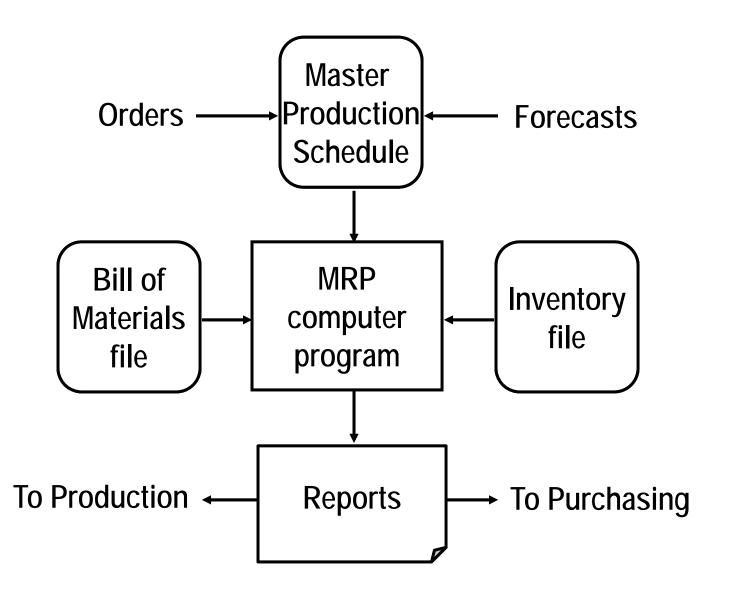






- Without an MRP system:
  - Component is ordered at time A, when the inventory level of the component hits reorder point, R
  - So, the component is received at time B.
  - However, the component is actually needed at time C, not B. So, the inventory holding cost incurred between time B and C is a wastage.
- With an MRP system:
  - We shall see in this lesson that given the production schedule of the finished goods and some other information (see the next slide), it is possible to predict the exact time, C when the component will be required. Order is placed carefully so that it is received at time C.

- MRP Inputs:
  - Master Production Schedule (MPS): The MPS of the finished product provides information on the net requirement of the finished product over time.
  - Bill of Materials: For each component, the bill of materials provides information on the number of units required, source of the component (purchase/ manufacture), etc. There are two forms of the bill of materials:
    - Product Structure Tree: The finished product is shown at the top, at level 0. The components assembled to produce the finished product is shown at level 1 or below. The sub-components used to produce the components at level 1 is



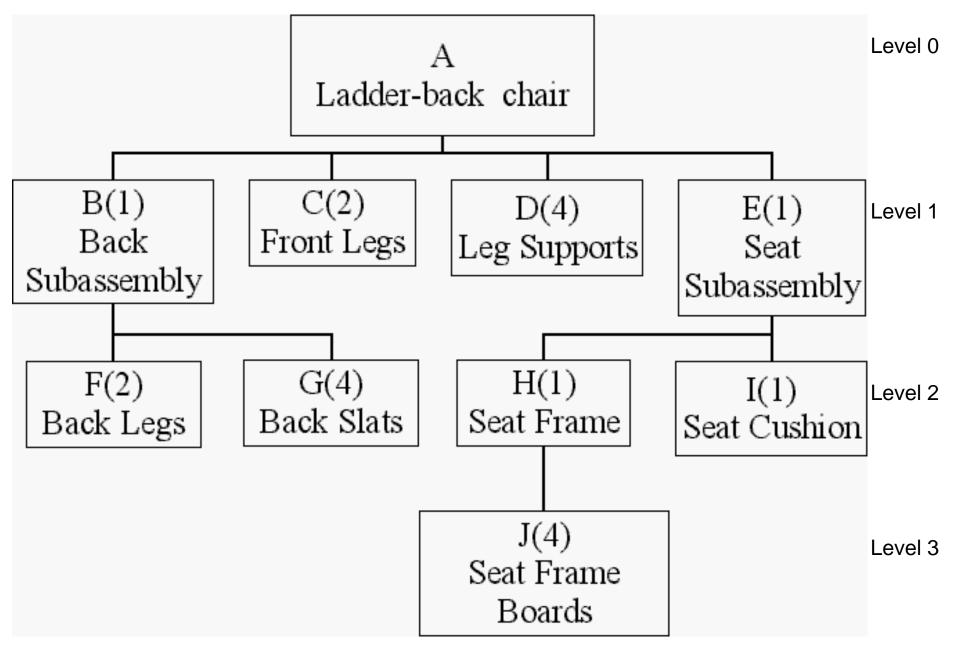
shown at level 2 or below, and so on.

The number in the parentheses shows the requirement of the item. For example, "G(4)" implies that 4 units of G is required to produce 1 unit of B.

The levels are important. The net requirements of the components are computed from the low levels to high. First, the net requirements of the components at level 1 is computed, then level 2, and so on.

- Bill of Materials: For each item, the name, number, source, and lead time of every component required is shown on the bill of materials in a tabular form.
- Inventory file: For each item, the number of units on hand is obtained from the inventory file.
- MRP Output:
  - Every required item is either produced or purchased.
    So, the report is sent to production or purchasing.

#### **Bill of Materials: Product Structure Tree**



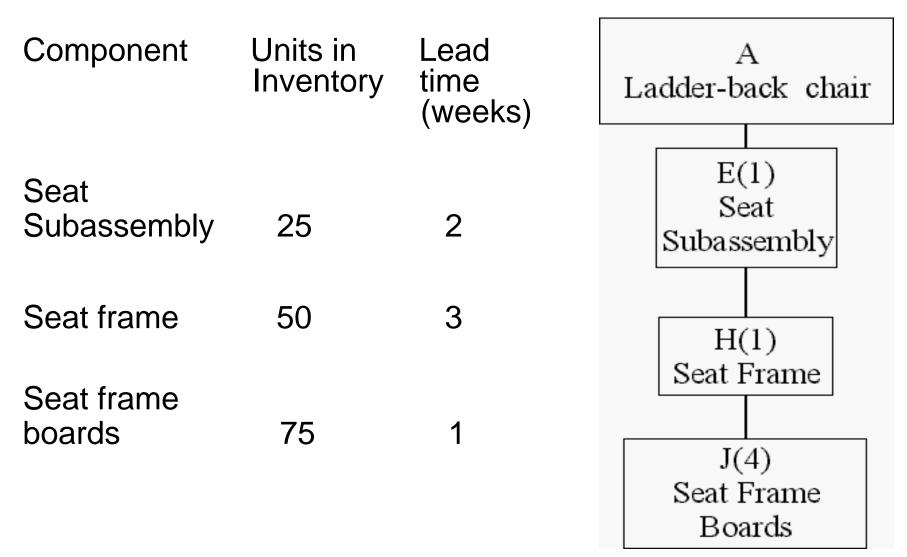
# **Bill of Materials**

	BILL OF MAT	<b>ERIALS</b>										
	Product Description: Lad	lder-back cha	ir									
	Item: A											
	Component Quantity Source											
Item	Description	Required										
В	Ladder-back	1	Manufacturing									
C	Front legs	2	Purchase									
D	Leg supports	4	Purchase									
E	Seat	1	Manufacturing									

### **Bill of Materials**

	BILL OF MAT	ERIALS									
	Product Description: Sea	t									
<i>Item</i> : E											
	Component	Quantity	Source								
Item	Description	Required									
H	Seat frame	1	Manufacturing								
Ι	Seat cushion	1	Purchase								

#### **On Hand Inventory and Lead time**



- Now, the MRP calculation will be demonstrated with an example.
- Suppose that 150 units of ladder-back chair is required.
- The previous slide shows a product structure tree with seat subassembly, seat frames, and seat frame boards.
   For each of the above components, the previous slide also shows the number of units on hand.
- The net requirement is computed from top to bottom. Since 150 units of ladder-back chair is required, and since 1 unit of seat subassembly is required for each unit of ladder-back chair, the gross requirement of seatsubassembly is 150×1 =150 units. Since there are 25 units of seat-subassembly in the inventory, the net requirement of the seat-subassembly is 150-25 = 125

units. Since 1 unit of seat frames is required for each unit of seat subassembly, the gross requirement of the seat frames is  $125 \times 1 = 125$  units. (*Note that although it* follows from the product structure tree that 1 unit of seat frames is required for each unit of ladder-back chair, the gross requirement of seat frames is not 150 units because each of the 25 units of seat-subassembly also contains 1 unit of seat frames.) Since there are 50 units of seat frames in the inventory, the net requirement of the seat frames is 125-50 = 75 units. The detail computation is shown in the next two slides.

• A similar logic is used to compute the time of order placement.

	Units
Quantity of ladder-back chairs to be produced	150
Gross requirement, seat subassembly	
Less seat subassembly in inventory	25
Net requirement, seat subassembly	
Gross requirement, seat frames	
Less seat frames in inventory	50
Net requirement, seat frames	
Gross requirement, seat frame boards	
Less seat frame boards in inventory	75
Net requirement, seat frame boards	

Assume that 150 units of ladder-back chairs are to be produced at the end of week 15

#### **MRP Calculation: Time of Order Placement**

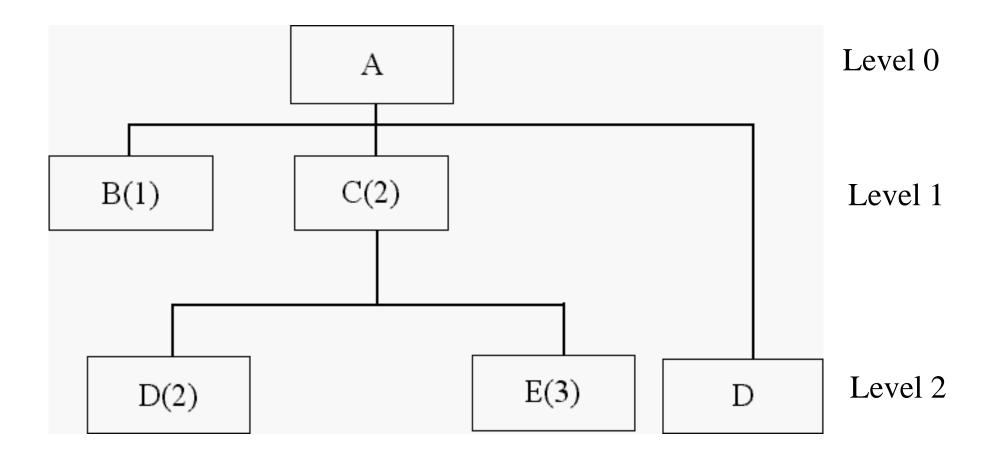
	Week
Complete order for seat subassembly	14
Minus lead time for seat subassembly	2
Place an order for seat subassembly	
Complete order for seat frames	
Minus lead time for seat frames	3
Place an order for seat frames	
Complete order for seat frame boards	
Minus lead time for seat frame boards	1
Place an order for seat frame boards	

Assume that 150 units of ladder-back chairs are to be produced at the end of week 15 and that there is a one-week lead time for ladder-back chair assembly

# **MRP Calculation: Some Definitions**

- Scheduled Receipts:
  - Items ordered prior to the current planning period and/or
  - Items returned from the customer
- Lot-for-lot (L4L)
  - Order quantity equals the net requirement
  - Sometimes, lot-for-lot policy cannot be used. There may be restrictions on minimum order quantity or order quantity may be required to multiples of 50, 100 etc.

**Example 1:** Each unit of A is composed of one unit of B, two units of C, and one unit of D. C is composed of two units of D and three units of E. Items A, C, D, and E have on-hand inventories of 20, 10, 20, and 10 units, respectively. Item B has a scheduled receipt of 10 units in period 1, and C has a scheduled receipt of 50 units in Period 1. Lot-for-lot (L4L) is used for Items A and B. Item C requires a minimum lot size of 50 units. D and E are required to be purchased in multiples of 100 and 50, respectively. Lead times are one period for Items A, B, and C, and two periods for Items D and E. The gross requirements for A are 30 in Period 2, 30 in Period 5, and 40 in Period 8. Find the planned order releases for all items.



	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross										
	Requirements										
A	Scheduled										
	receipts										
LT=	On hand from										
	prior period										
	Net										
	requirements										
Q=	Time-phased Net										
	Requirements										
	Planned order										
	releases										
	Planned order										
	delivery										20

	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross		20			30			40		
	Requirements		30			50			40		
A	Scheduled										
	receipts										
LT=	On hand from	•									
1	prior period	20									
1	Net										
WK	requirements										
Q=	Time-phased Net										
	Requirements										
L4L	Planned order										
	releases										
	Planned order										
	delivery										20

All the information above are given.

	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross		30			30			40		
	Requirements		50			50			40		
A	Scheduled										
	receipts										
LT=	On hand from										
1	prior period	20	20								
1	Net										
WK	requirements										
Q=	Time-phased Net										
	Requirements										
L4L	Planned order										
	releases										
	Planned order										
	delivery										20

20 units are just transferred from Period 1 to 2.

30

	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross		30			30			40		
	Requirements		30			50			40		
A	Scheduled										
	receipts										
LT=	On hand from	•	•								
1	prior period	20	20								
1	Net		10								
WK	requirements		10								
Q=	Time-phased Net										
	Requirements	10									
L4L	Planned order	10									
	releases	10									
	Planned order		10								
	delivery		10								31

The net requirement of 30-20=10 units must be ordered in week  $1^{31}$ .

	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross		30			30			40		
	Requirements		50			50			40		
A	Scheduled										
	receipts										
LT=	On hand from	•	•	0	0						
1	prior period	20	20	0	0	0					
$\begin{vmatrix} 1 \\ \mathbf{W} \end{matrix}$	Net		10								
WK	requirements		10								
Q=	Time-phased Net										
	Requirements	10									
L4L	Planned order	10									
	releases	10									
	Planned order		10								
	delivery		10								20

On hand in week 3 is (20+10)-30=0 unit.

	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross		30			30			40		
	Requirements		30			50			40		
A	Scheduled										
	receipts										
LT=	On hand from				0						
1	prior period	20	20	0	0	0					
1	Net		10			20					
WK	requirements		10			30					
Q=	Time-phased Net				20						
	Requirements	10			30						
L4L	Planned order	10			30						
	releases	10			$\sim$						
	Planned order		10			30					
	delivery		10			50					33

The net requirement of 30-0=30 units must be ordered in week 4.<sup>33</sup>

	Period	1	2	3	4	5	6	7	8	9	10
Item	Gross		20			30			40		
	Requirements		30			50			40		
A	Scheduled										
	receipts										
LT=	On hand from	•	•	0			0	0			
1	prior period	20	20	0	0	0	0	0	0		
$\begin{vmatrix} 1 \\ \mathbf{W} \end{matrix}$	Net		10			30			40		
WK	requirements		10			50			40		
Q=	Time-phased Net				30			40			
	Requirements	10			50			40			
L4L	Planned order	10			30			40			
	releases	10			30			40			
	Planned order		10			30			40		
	delivery		10			50			40		34

The net requirement of 40-0=30 units must be ordered in week 7.

Period	1	2	3	4	5	6	7	8	9	10
Gross		20			20			40		
Requirements		50			50			40		
Scheduled										
receipts										
On hand from	•		0			0	0		0	
prior period	20	20	0	0	0	0	0	0	0	0
Net		10			20			40		
requirements					50			40		
Time-phased Net	10			20						
Requirements	10			50			40			
Planned order	10			30			40			
releases				30			40			
Planned order		10			30			$\mathbf{A}$		
delivery		10			50			40		35
	Gross Requirements Scheduled receipts On hand from prior period Net Net requirements Time-phased Net Requirements Planned order releases	GrossIRequirementsIScheduledIScheduledIreceiptsIOn hand from20Net20NetIrequirementsITime-phased Net10Requirements10Planned order10Planned order10Planned order10Planned order10	Gross Requirements30Requirements30Scheduled receipts4receipts4On hand from prior period20Net requirements20Net requirements10Time-phased Net Requirements10Planned order releases10Planned order releases10Net releases10	Gross Requirements30Scheduled receiptsIScheduled receiptsIOn hand from prior period202020Net requirementsITime-phased Net RequirementsI10IPlanned order releases10Planned order1010II <tdi< td="">I<tdi< td="">I</tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<></tdi<>	Gross Requirements3030Scheduled receiptsIIOn hand from prior period20200Net requirementsII00Net requirementsII0ITime-phased Net Requirements10I30Planned order releases10I30Planned order releases10I30	Gross Requirements303030Scheduled receiptsOn hand from prior period2020000Net requirements10-30Time-phased Net Requirements10-30-Planned order releases10-30-Planned order releases10-30-Planned order releases10-30-	Gross Requirements303030Scheduled receiptsOn hand from prior period202000Net requirements10-30Time-phased Net Requirements10-30-Planned order releases1030Planned order101030-	Gross Requirements30303030Scheduled receiptsOn hand from prior period20200000Net requirements1030Time-phased Net Requirements1030-40Planned order releases1030-40	Gross Requirements3030303040Scheduled receipts40On hand from prior period2020000000Net requirements10-30-40Time-phased Net Requirements10-30-40Planned order releases10-30-40Planned order releases10-30-40	Gross Requirements30303040Scheduled receipts40On hand from prior period2020000000Net requirements10304040Time-phased Net Requirements10304040-Planned order releases10304040-

The net requirement of 40-0=30 units must be ordered in week 7.<sup>33</sup>

Period		1	2	3	4	5	6	7	8	9	10
Item	Gross										
	Requirements										
B	Scheduled										
	receipts										
LT=	On hand from										
	prior period										
	Net										
	requirements										
Q=	Time-phased Net										
	Requirements										
	Planned order										
	releases										
	Planned order										
	delivery										26

Period		1	2	3	4	5	6	7	8	9	10
Item	Gross										
	Requirements										
C	Scheduled										
	receipts										
LT=	On hand from										
	prior period										
	Net										
	requirements										
Q=	Time-phased Net										
	Requirements										
	Planned order										
	releases										
	Planned order										
	delivery										27

Period		1	2	3	4	5	6	7	8	9	10
Item	Gross										
	Requirements										
D	Scheduled										
	receipts										
LT=	On hand from										
	prior period										
	Net										
	requirements										
Q=	Time-phased Net										
	Requirements										
	Planned order										
	releases										
	Planned order										
	delivery										20

Period		1	2	3	4	5	6	7	8	9	10
Item	Gross										
	Requirements										
E	Scheduled										
	receipts										
LT=	On hand from										
	prior period										
	Net										
	requirements										
Q=	Time-phased Net										
	Requirements										
	Planned order										
	releases										
	Planned order										
	delivery										

# **READING AND EXERCISES**

Lesson 21

Reading:

Section 7.1 pp. 355-364 (4<sup>th</sup> Ed.), pp. 346-358 (5<sup>th</sup> Ed.)

Exercise:

4 and 9 pp. 364-366 (4<sup>th</sup> Ed.), pp. 356-358 (5<sup>th</sup> Ed.)